

# Supervised Learning In Quest SLIQ

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# Introduction

## What is SLIQ?



- SLIQ (Supervised Learning in Quest) is a high speed and flexible decision tree classifier that allows to sort and interpret data.
- SLIQ can reduce costs using efficient and pre-sorting decision trees to sort through larger data sets while accounting for differences in data types.
- This maintains competitive accuracy with the ability to scale and interpret larger data sets with multiple classes and attributes.
- SLIQ Algorithm can be divided into 3 steps, pre-sorting the sample, processing evaluation on splits, and updating the class list.

## Gini Index



- SLIQ uses a training set and a Gini split to prepare the data for the decision tree algorithm. These equations are what make SLIQ a, supervised learning, algorithms as the data is pre-sorted and pruned.
- For training set L with n distinct classes the equation:

Attribute Value < P	A	В
L	al	a2
R	b1	b2

Histogram example

$$Gini(L) = 1 - \sum j = 1 \dots n P^2 j$$
  
- pj is the relative frequency of j.

$$\begin{aligned} &Gini\ Index = \frac{a1+a2}{n}\left[1-\left(\frac{a1}{a1+a2}\right)^2-\left(\frac{a2}{a1+a2}\right)^2\right] + \\ &\frac{b1+b2}{n}\left[1-\left(\frac{b1}{b1+b2}\right)^2-\left(\frac{b2}{b1+b2}\right)^2\right] (5) \quad \text{with data classes a and b} : \end{aligned}$$



# Example

# Training Data Table



Credit Score	Married Status	Debt Existence	House Own	Credit Card
302	Υ	Υ	N	N
353	Υ	Υ	N	N
420	N	N	Υ	Υ
545	N	Υ	N	N
610	Υ	N	N	N
610	N	N	Υ	Υ
710	N	N	N	Υ
720	N	Υ	Υ	N
780	Υ	Υ	Υ	Υ
850	N	N	Y	Υ

## Pre-Sorting



Credit Score	Index
302	1
353	2
420	3
545	4
610	5
610	6
710	7
720	8
780	9
850	10

Married Status	Index
Υ	1
Υ	2
Y	5
Y	9
N	3
N	4
N	6
N	7
N	8
N	10

Debt Existence	Index
Υ	1
Y	2
Υ	4
Υ	8
Y	9
N	3
N	5
N	6
N	7
N	10

House Owned	Index
Υ	3
Υ	6
Υ	8
Υ	9
Υ	10
N	1
N	2
N	4
N	5
N	7

- Credit Score attribute does not have predictive power since they can be any number (continuous).

## Gini Index



- -Finding Gini index for each attribute, in order to find the root node.
- -Gini index for Married status attribute =  $P(M = y) * \{1 [P(M = y \& C = y)^2 + P(M = y \& C = n)^2] \} + P(M = n) * \{1 [P(M = n \& C = y)^2 + P(M = n \& C = n)^2] \} = 0.41$
- -Gini index for Debt existence attribute = 0.34
- -Gini index for House own attribute = 0.31
- -House own attribute is used for the root node.

# Processing Evaluation on Splits



House Owned	Index		Married Status	Index	Debt Existence	Index		Credit Card	Index
Υ	3		Y	1	Υ	1	,	N	3
Υ	6		Υ	2	Υ	2		N	6
Υ	8		Y	5	Υ	4		Υ	7
Υ	9		Υ	9	Υ	8		N	9
Υ	10		N	3	Υ	9		N	10
N	1		N	4	N	3		Υ	1
N	2	,	N	6	N	5		Υ	2
N	4		N	7	N	6		N	4
N	5		N	8	N	7		Y	5
N	7		N	10	N	10		Υ	8

- Using the root node create and determine the sub node.

# Updating the Class List.



1	N	2
-	N	

House Own	Married Status	Debt Existence	Credit Card
Υ	N	N	Υ
Υ	N	N	Υ
Υ	N	Υ	N
Υ	Υ	Υ	Υ
Υ	N	N	Υ

N3

House Own	Married Status	Debt Existence	Credit Card
N	Υ	Υ	N
N	Υ	Υ	N
N	N	Υ	N
N	Υ	N	N
N	N	N	Υ

- Previous steps repeat for each sub nodes.

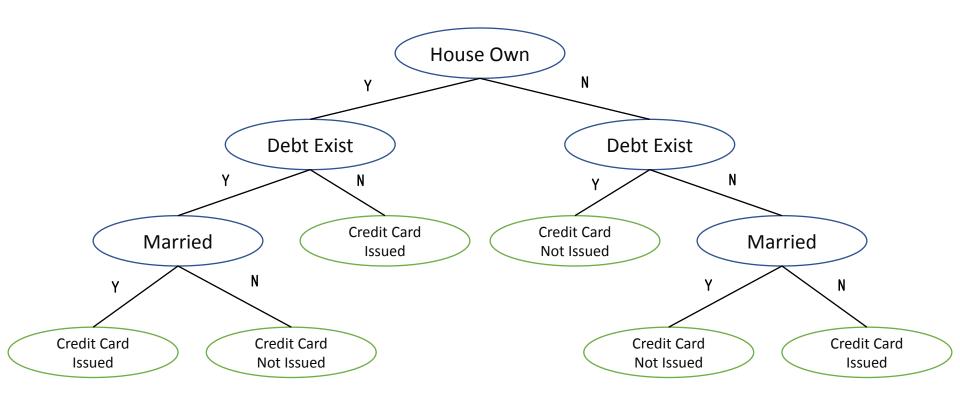
## Gini Index for Sub Nodes N2 and N3

- N2: Gini index for Married status attribute = 0.3 Gini index for Debt existence attribute = 0.2
- Debt existence attribute is used on sub node N2.
- N3: Gini index for Married status attribute = 0.2 Gini index for Debt existence attribute = 0.2
- Either Debt existence or Married status attribute can be used on sub node N3.

## Decision Tree



- Decision tree made based on the training data:





```
1 #include "msp.h"
                                                                             i 58
                                                                                          if (input[i][3] == 1)
 2 #include <math.h>
                                                                               59
 3 #include <stdio.h>
                                                                               60
                                                                                               result[i].house = true;
 4 #include <stdlib.h>
                                                                               61
 5 #include <stdint.h>
                                                                               62
                                                                                          else
 6 #include <stdbool.h>
                                                                               63
                                                                               64
                                                                                              result[i].house = false;
 8 void UARTO init(void);
                                                                               65
                                                                               66
10 // structure for the attribute
                                                                               67
                                                                                           if (input[i][4] == 1)
11 typedef struct entry
                                                                               68
12 {
                                                                               69
                                                                                              result[i].credit_c = true;
13
       int credit s;
                                                                               70
14
       bool married;
                                                                               71
                                                                                          else
15
       bool debt;
                                                                               72
16
       bool house;
                                                                               73
                                                                                               result[i].credit_c = false;
17
       bool credit c;
                                                                               74
18 } entry;
                                                                               75
                                                                               76
20 // structure for counting each attribute
                                                                               77
                                                                                      return result;
21 typedef struct totals
                                                                               78 }
22 {
                                                                               79
23
       double married:
                                                                               80 // function to count the total number of 1s (yes) for each attribute
       double debt;
24
                                                                               81// of the data (return type: totals structure)
25
       double house;
                                                                                82 totals get_totals(entry* entries)
26
       double credit c;
                                                                               83 {
27 } totals;
                                                                                      totals result = {0};
                                                                               84
28
                                                                               85
                                                                                      int i;
29 // function to analyze the input data (return type: entry structure)
                                                                               86
                                                                                      for (i = 0; i < 10; ++i)
30 entry* parse input(double input[10][5])
                                                                               87
31 {
                                                                               88
                                                                                          if (entries[i].married == true)
32
       // allocate the structure 'result' with memory size 100
                                                                               89
33
       entry* result = malloc(100);
                                                                             i 90
                                                                                               result.married += 1;
34
       int i;
                                                                               91
35
       // summarize each attribute depending on each attributes' value
                                                                               92
                                                                                          if (entries[i].debt == true)
36
       for (i = 0; i < 10; i++)
                                                                               93
37
                                                                               94
                                                                                               result.debt += 1;
38
           result[i].credit_s = input[i][0];
                                                                               95
39
                                                                               96
                                                                                          if (entries[i].house == true)
40
           if (input[i][1] == 1)
                                                                               97
41
                                                                             i 98
                                                                                               result.house += 1;
42
               result[i].married = true;
                                                                               99
43
                                                                              100
                                                                                          if (entries[i].credit c == true)
44
           else
                                                                              101
45
                                                                             i 102
                                                                                              result.credit_c += 1;
46
               result[i].married = false;
                                                                              103
47
                                                                              104
48
                                                                              105
49
           if (input[i][2] == 1)
                                                                              106
                                                                                      return result;
50
                                                                              107 }
51
               result[i].debt = true;
                                                                               108
52
           }
                                                                              109
53
           else
                                                                              110 void main(void)
54
                                                                              111 {
55
               result[i].debt = false;
                                                                              112
                                                                                      WDT_A->CTL = WDT_A_CTL_PW | WDT_A_CTL_HOLD;// stop_watchdog_timer
56
```

168



```
// training data table as a 2d array
115
        // Credit Score
                            Married Status Debt Status
                                                                       Credit Card
                                                            House Own
116
        11
                                   Yes = 1
                                               True = 1
                                                              Yes = 1
                                                                            Yes = 1
117
        11
                                                 No = 0
                                                                             No = 0
                                    No = 0
                                                               No = 0
118
        double input[10][5] =
119
120
         {302,1,1,0,0},
121
         {353,1,1,0,0},
122
         {420,0,0,1,1},
123
         {545,0,1,0,0},
124
         {610,1,0,0,0},
125
         {610,0,0,1,1},
126
         {710,0,0,0,1},
127
         {720,0,1,1,0},
128
         {780,1,1,1,1},
129
         {850,0,0,1,1}
130
        };
131
132
        entry* entries = parse input(input);
133
134
        totals total = get totals(entries);
135
136
        //calculate gini for married
137
        double prob married y = total.married / 10;
138
        double prob married n = 1 - prob married v;
139
140
        double married y credit c y = 0;
141
        double married n credit c y = 0;
142
143
        int i:
144
        for (i = 0; i < 10; ++i)
145
146
            if (entries[i].married == true && entries[i].credit c == true)
147
            {
148
                married y credit c y += 1;
149
150
151
            if (entries[i].married == false && entries[i].credit c == true)
152
            {
153
                married n credit c y += 1;
154
            }
155
156
157
        double prob married y credit c y = married y credit c y / total.married;
158
        double prob married y credit c n = 1 - prob married y credit c y;
159
160
161
        double prob_married_n_credit_c_y = married_n_credit_c_y / (10 - total.married);
162
        double prob married n credit c n = 1 - prob married n credit c y;
163
164
        double gini married = ((prob married v) * (1 - (pow(prob married v credit c y, 2) +
165
                         pow(prob married v credit c n, 2)))) + ((prob married n) *
166
                 (1 - (pow(prob married n credit c y, 2) + pow(prob married n credit c n, 2))));
167
```



```
// calculate gini for debt
169
170
        double prob debt v = total.debt / 10;
171
        double prob debt n = 1 - prob debt y;
172
173
        double debt y credit c y = 0;
174
        double debt n credit c y = 0;
175
176
        for (i = 0; i < 10; ++i)
177
178
            if (entries[i].debt == true && entries[i].credit c == true)
179
180
                debt_y_credit_c_y += 1;
181
            }
182
183
            if (entries[i].debt == false && entries[i].credit c == true)
184
185
                debt_n_credit_c_y += 1;
186
187
188
189
        double prob debt v credit c y = debt v credit c y / total.married;
190
        double prob debt v credit c n = 1 - prob debt v credit c v;
191
192
        double prob_debt_n_credit_c_y = debt_n_credit_c_y / (10 - total.debt);
193
        double prob debt n credit c n = 1 - prob debt n credit c v;
194
195
        double gini debt= ((prob debt y) * (1 - (pow(prob debt y credit c y, 2)
196
               + pow(prob debt y credit c n, 2)))) + ((prob debt n) *
197
               (1 - (pow(prob debt n credit c y, 2) + pow(prob debt n credit c n, 2))));
198
199
200
        // calculate gini for house
201
        double prob house y = total.house / 10;
202
        double prob house n = 1 - prob house v;
203
204
        double house y credit c y = 0;
205
        double house n credit c y = 0;
206
207
        for (i = 0; i < 10; i++)
208
209
            if (entries[i].house == true && entries[i].credit c == true)
210
            {
211
                house y credit c v += 1;
 212
 213
214
            if (entries[i].house == false && entries[i].credit c == true)
215
216
                house n credit c v += 1;
217
            }
218
219
220
        double prob house y credit c y = house y credit c y / total.house;
221
        double prob house y credit c n = 1 - prob house y credit c y;
222
223
        double prob house n credit c y = house n credit c y / (10 - total.house);
224
        double prob house n credit c n = 1 - prob house n credit c v:
```



```
225
226
        double gini house = ((prob house y) * (1 - (pow(prob house y credit c y, 2)
227
                + pow(prob house y credit c n, 2)))) + ((prob house n) *
228
                    (1 - (pow(prob_house_n_credit_c_y, 2) + pow(prob_house_n_credit_c_n, 2))));
 229
 230
        // integers and char to represents the decimal points for each gini index
 231
        int a, b, c, d, e, f;
 232
        char A, B, C, D, E, F;
 233
234
        a = gini married * 10;
235
        A = (char)a + '0';
 236
        b = (gini married * 100) - (a * 10);
 237
        B = (char)b + '0';
 238
239
        c = gini debt *10;
240
        C = (char)c + '0';
241
        d = (gini debt * 100) - (c * 10);
242
        D = (char)d + '0';
 243
244
        e = gini house * 10;
245
        E = (char)e + '0';
246
        f = (gini house * 100) - (e * 10);
247
        F = (char)f + '0';
 248
249
        int x = 0;
 250
 251
        UARTO init();
 252
 253
            // print out each gini index to the terminal to decide which attribute
 254
            // to be used for splitting the decision tree
 255
 256
            // first attribute
 257
            while(!(EUSCI_A0->IFG & 0x02)) { } /* wait for transmit buffer empty */
 258
                                                /* send a char */
            EUSCI A0->TXBUF = '1';
 259
            while(!(EUSCI_A0->IFG & 0x02)) { }
            EUSCI A0->TXBUF = ':';
 260
                                                /* send a char */
 261
             while(!(EUSCI_A0->IFG & 0x02)) { }
 262
            EUSCI_A0->TXBUF = ' ';
                                                /* send a char */
 263
            while(!(EUSCI_A0->IFG & 0x02)) { }
 264
             EUSCI A0->TXBUF = '0';
                                                /* send a char */
265
            while(!(EUSCI_A0->IFG & 0x02)) { }
 266
             EUSCI_A0->TXBUF = '.';
                                                /* send a char */
 267
            while(!(EUSCI_A0->IFG & 0x02)) { }
 268
             EUSCI A0->TXBUF = A;
                                       /* send a char */
 269
            while(!(EUSCI_A0->IFG & 0x02)) { }
 270
            EUSCI A0->TXBUF = B;
271
            while(!(EUSCI A0->IFG & 0x02)) { }
 272
             EUSCI A0->TXBUF = '\t';
 273
 274
 275
 276
            // second attribute
277
            while(!(EUSCI A0->IFG & 0x02)) { } /* wait for transmit buffer empty */
                                                /* send a char */
 278
            EUSCI A0->TXBUF = '2';
279
             while(!(EUSCI_A0->IFG & 0x02)) { }
```



```
279
            while(!(EUSCI A0->IFG & 0x02)) { }
 280
            EUSCI A0->TXBUF = ':';
281
            while(!(EUSCI A0->IFG & 0x02)) { }
 282
             EUSCI_A0->TXBUF = ' ';
283
            while(!(EUSCI_A0->IFG & 0x02)) { }
 284
             EUSCI A0->TXBUF = '0';
 285
            while(!(EUSCI A0->IFG & 0x02)) { }
 286
             EUSCI A0->TXBUF = '.';
287
            while(!(EUSCI_A0->IFG & 0x02)) { }
 288
             EUSCI_A0->TXBUF = C;
 289
            while(!(EUSCI A0->IFG & 0x02)) { }
 290
             EUSCI A0->TXBUF = D;
 291
            while(!(EUSCI_A0->IFG & 0x02)) { }
 292
             EUSCI A0->TXBUF = '\t';
 293
 294
 295
            // third attribute
 296
            while(!(EUSCI A0->IFG & 0x02)) { } /* wait for transmit buffer empty */
 297
            EUSCI_A0->TXBUF = '3';
 298
            while(!(EUSCI A0->IFG & 0x02)) { }
 299
            EUSCI A0->TXBUF = ':';
 300
            while(!(EUSCI_A0->IFG & 0x02)) { }
 301
             EUSCI A0->TXBUF = ' ';
302
            while(!(EUSCI_A0->IFG & 0x02)) { }
 303
             EUSCI A0->TXBUF = '0';
304
            while(!(EUSCI A0->IFG & 0x02)) { }
 305
             EUSCI A0->TXBUF = '.';
306
            while(!(EUSCI A0->IFG & 0x02)) { }
 307
             EUSCI_A0->TXBUF = E;
 308
            while(!(EUSCI_A0->IFG & 0x02)) { }
 309
             EUSCI A0->TXBUF = F;
 310
            while(!(EUSCI A0->IFG & 0x02)) { }
 311
            EUSCI A0->TXBUF = '\t';
 312
313
            while(1){}
314 }
 315
 316 void UARTO_init(void)
 317 {
 318
         EUSCI A0->CTLW0 |= 1;
                                    /* put in reset mode for config */
 319
         EUSCI A0->MCTLW = 0;
                                    /* disable oversampling */
        EUSCI_A0->CTLW0 = 0x0081; /* 1 stop bit, no parity, SMCLK, 8-bit data */
 320
 321
        EUSCI A0->BRW = 26;
                                    /* 3,000,000 / 115200 = 26 */
                                    /* P1.3, P1.2 for UART */
 322
        P1->SEL0 |= 0x0C;
 323
        P1->SEL1 &= ~0x0C;
 324
        EUSCI A0->CTLW0 &= ~1;
                                    /* take UART out of reset mode */
 325 }
 326
```

Name	Туре	Value	Location
(×)= A	unsigned char	52 '4'	0x2000FFE4
(x)= a	int	4	0x2000FFC8
(×)= B	unsigned char	49 '1'	0x2000FFE5
(×)= b	int	1	0x2000FFCC
(×)= C	unsigned char	51 '3'	0x2000FFE6
(x)= C	int	3	0x2000FFD0
(×)= D	unsigned char	52 '4'	0x2000FFE7
(×)= d	int	4	0x2000FFD4
(x)= debt_n_credit_c_y	double	4.0	0x2000FF48
(x)= debt_y_credit_c_y	double	1.0	0x2000FF40
(×)= E	unsigned char	51 '3'	0x2000FFE8
(x)= e	int	3	0x2000FFD8
→ entries	struct entry *	0x20000008 {credit_s=302,married=1 "\x01",de	0x2000FFC0
(x)= F	unsigned char	49 '1'	0x2000FFE9
(x)= f	int	1	0x2000FFDC
(x)= gini_debt	double	0.34750000000000003	0x2000FF70
(×)= gini_house	double	0.319999999999995	0x2000FFB8
(x)= gini_married	double	0.4166666666666674	0x2000FF28
(x)= house_n_credit_c_y	double	1.0	0x2000FF90
(x)= house_y_credit_c_y	double	4.0	0x2000FF88
(×)= i	int	10	0x2000FFC4
> 🏉 input	double[10][5]	[[302.0,1.0,1.0,0.0,0.0],[353.0,1.0,1.0,0.0,0.0],[42	0x2000FD38
(x)= married_n_credit_c_y	double	4.0	0x2000FF00
(x)= married_y_credit_c_y	double	1.0	0x2000FEF8
(x)= prob_debt_n	double	0.5	0x2000FF38
(x)= prob_debt_n_credit_c_n	double	0.2000000000000007	0x2000FF68
(x)= prob_debt_n_credit_c_y	double	0.79999999999993	0x2000FF60
(x)= prob_debt_y	double	0.5	0x2000FF30
(x)= prob_debt_y_credit_c_n	double	0.75	0x2000FF58
(x)= prob_debt_y_credit_c_y	double	0.25	0x2000FF50
(x)= prob_house_n	double	0.5	0x2000FF80
(x)= prob_house_n_credit_c_n	double	0.8000000000000004	0x2000FFB0
(x)= prob_house_n_credit_c_y	double	0.19999999999998	0x2000FFA8
(x)= prob_house_y	double	0.5	0x2000FF78
(x)= prob_house_y_credit_c_n	double	0.2000000000000007	0x2000FFA0
(x)= prob_house_y_credit_c_y	double	0.79999999999999	0x2000FF98
(x)= prob_married_n	double	0.6000000000000000	0x2000FEF0
(x)= prob_married_n_credit_c_n	double	0.33333333333333	0x2000FF20
(x)= prob_married_n_credit_c_y	double	0.666666666666663	0x2000FF18
(x)= prob_married_y	double	0.399999999999997	0x2000FEE8
(x)= prob_married_y_credit_c_n	double	0.75	0x2000FF10
(x)= prob_married_y_credit_c_y	double	0.25	0x2000FF08
> 🥭 total	struct totals	{married=4.0,debt=5.0,house=5.0,credit_c=5.0}	0x2000FEC8
(x)= x	int	0	0x2000FFE0



# Demo